

# Harmonic pollution control of electrical networks: Comparative study of controls, by Pulse Width Modulation, Duty Cycle Modulation and Symmetrical Linear Duty Cycle Modulation of the three-phase shunt active Parallel filters

Fabrice Biloa Assolo<sup>1</sup>, Charles Hubert Kom<sup>1, 2</sup>, Arnaud Nanfak<sup>2</sup>, Gildas Martial Ngaleu<sup>2</sup>

<sup>1</sup>Research Laboratory of Computer Science Engineering and Automation  
Higher Normal School of Technical Education,

University of Douala, Po Box 2701 Douala, Cameroon

<sup>2</sup>Laboratory of Energy, Materials, Modelling and Methods,  
Higher National Polytechnic School of Douala

University of Douala, Po Box 2701 Douala, Cameroon

<sup>1</sup>fabricebiloa@yahoo.fr, <sup>2</sup>charleshubert.kom@gmail.com, <sup>2</sup>nanfak.arnaud@yahoo.fr, <sup>2</sup>gmngaleu@yahoo.fr

**Abstract** – The increasing use on electrical networks of consumer electronic devices (televisions, computers) and industrial electronic devices (variable speed drives, high efficiency lighting) pollutes these networks by harmonic currents and voltages. The three-phase active shunt filter is a modern solution for the remediation of three-phase electrical networks. Better pollution control requires proper sizing of the active shunt filter. Indeed, the capacity and adaptability of the filter reside in the quality of the control of the switches of the inverter constituting it. In this article we are interested in controlling inverters. A comparative study of Pulse Width Modulator (PWM) controls, Duty Cycle Modulation inverter (DCM) control and Symmetrical Linear Duty Cycle Modulation (SLDCM) control in a three-phase network. The study shows that the DCM inverter gives the best results with regard to the reduction of harmonic pollution, and therefore of the quality of the network.

**Keywords:** *shunt active parallel filter, Harmonic pollution, PWM control, DCM control, SLDCM control*

## I. INTRODUCTION

The development of power electronics and the increase in the powers involved as well as the flexible use of semiconductors, an encouraged electrical engineer to undertake important associations of static converters power to electrical machines. These devices are usually loads that are not linear, which absorb a non-sinusoidal current and behave like harmonic generators. Of moreover, they sometimes consume reactive energy. Therefore, the waveform of

the current of the source loses its sinusoidal shape and we obtain also a degradation of the power factor. Through therefore, distributors of electrical energy see themselves therefore obliged to impose standards and protect themselves against these disturbances. One of the solutions used is passive filtering: it consists in trapping the currents harmonics in LC circuits, tuned to the ranks of harmonics to be filtered. Rows 5 and 7 are the most commonly filtered. However, this solution is moderately effective [1] - [2]. Common use of devices power electronics, made it possible to design self-adapting harmonic elimination devices called active compensators harmonics, or active filters. These filters the main objective of the assets is to compensate for harmonic currents injected into the network [3] [4] [5]. Our work then turned to the study of the control-command block of the active filter. There are several types of control of three-phase shunt filters for this purpose which have been presented in the literature. There are several techniques to control the compensating current injection such as a Pulse Width Modulation (PWM) Duty Cycle Modulation (DCM) and new duty-cycle modulator structures namely Symmetrical Linear DCM (SLDCM). PWM technique is a modulation technique in which the frequency can be either constant or variable[6]. In constant frequency PWM method, the frequency is constant and the ON time changes according to the modulating signal. It can be produced by comparing a reference signal with a carrier signal[6]. In variable frequency PWM method, the frequency is variable and ON time or OFF time is constant. In variable

frequency PWM method, the frequency is variable and ON time or OFF time is constant. There are several different PWM techniques, differing in their methods of implementation. The basics PWM topologies including single PWM produced by comparing rectangular reference wave with triangular carrier wave, the multiple PWM and the Sinusoidal PWM (SPWM) using sinusoidal reference wave and triangular carrier wave [7].

The duty cycle modulation (DCM) is a modulation in which an input signal  $x$  is transformed into a train of switching wave where duty cycle and period of the modulated signal vary simultaneously according to control signal [8] [7]. The DCM technique has been used in several application areas.

From instrumentation to process control, including Signal processing. Thus, a scientific article on the application of the principle of modulation of duty cycle in instrumentation has been published [9]. In this article, a class of new DCM is investigated. It used the analog signal processing techniques with a simple operational amplifier circuit. The first papers to use DCM as an analog-to-digital converter are [10] [11]. These two papers respectively presented the feasibility of analog-to-digital conversion by DCM via virtual simulations and the multi-channel version of A/D conversion based on the use of duty cycle modulator cells in parallel, each used as a circuit.

In [12], buck converters use the DCM control technique. In this article, analytical developments, numerical analysis, virtual simulations and experimentation have demonstrated that DCM control system provides better characteristics compared to standard PWM techniques, so DCM control can be considered as a new perspective of control in power electronics and control engineering [13], with a

possible extension to other CC-CC converters [14], even to the important class of DC-AC inverters [15].

The article [16] makes the comparative study of IGBT controls between DCM and hysteresis in a three-phase network, it emerges that the DCM control offers the best performance in terms of harmonic rate reduction.

The new DCM modulator structures are proposed in [17]. These are Symmetric Linear DCM (SLDCM) and General Linear DCM (GLDCM). These two structures consist of integrator circuits, a hysteresis comparator and advantages of PWM and DCM circuits.

In this paper, our objective is to make a comparative study followed by simulation in the software MATLAB / SIMULINK, of the controls by PWM, DCM of the inverter and SLDCM of an SAPF (Shunt Active parallel Filter) for harmonic pollution control application.

The article is organized as follows. In section II, we present the methodology used. In section III, we present the simulation results. And we end with a conclusion where we highlight the value of this best-performing ordering strategy.

## II. METHOD

### A. Principle of parallel active filter

This filter is connected in parallel on the network. The principle of the parallel active filter consists in generating currents in opposition of phase to the harmonic currents existing on the network and created by the nonlinear loads. In this way, the current supplied by the energy source remains sinusoidal. The parallel active filter consists of two blocks: the power part and the control-command part Figure.1.

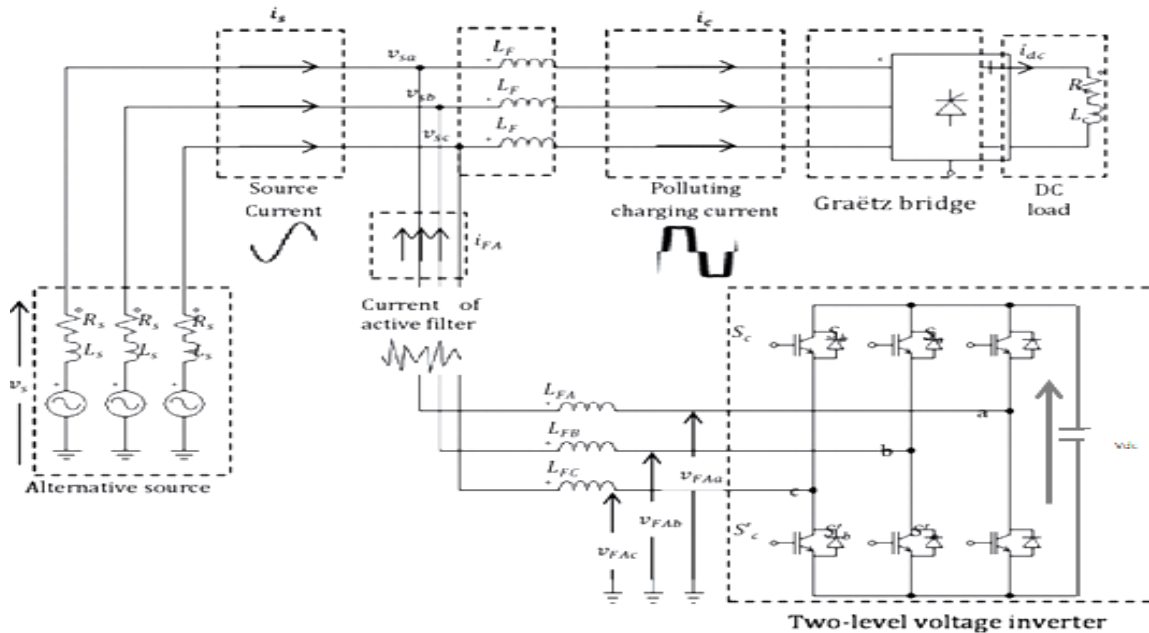


Figure 1: Principle of the parallel active filter [18]

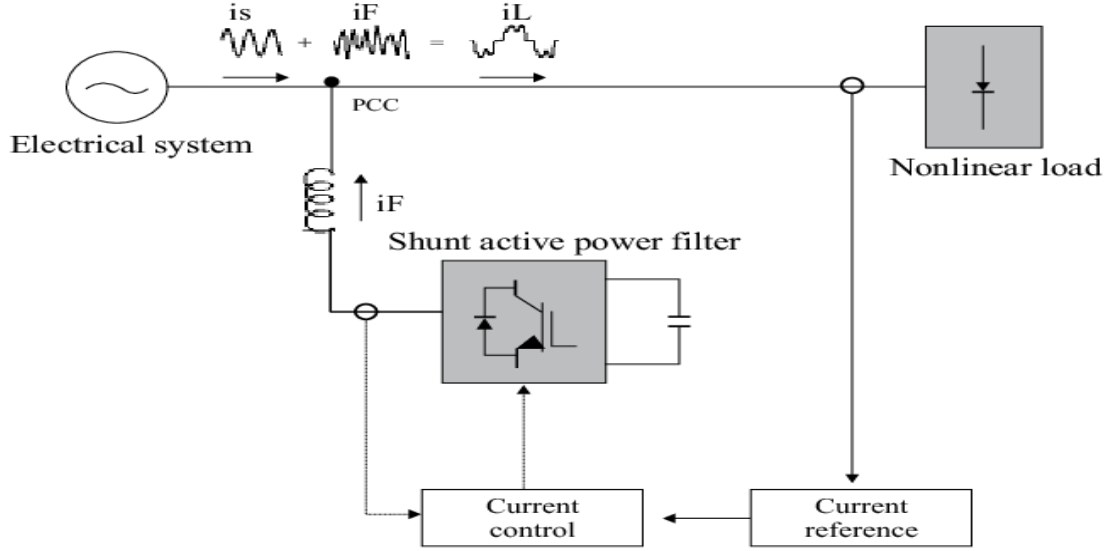


Figure 2: Main blocks in the electrical circuit for a shunt active power filter

Concerning Figure 2, we can identify the main block of our study: the current control because it is in this block that we will apply in turn the command PWM, DCM inverter and SLDCM to switch the IGBTs of the inverter. In the second current reference block, we will apply the instantaneous powers algorithm to identify the reference currents.

#### B. Theory of instantaneous powers

The instantaneous active and reactive power method was developed by Akagi [19] and uses the Concordia transformation of phase-to-neutral voltages  $V_s$  and line currents  $I_s$ , in order to calculate instantaneous active and reactive powers. The principle of this classical method is now briefly described. Let respectively be the phase-to-neutral voltages of a three-phase network without zero sequence (connected to a polluting load) and the three load currents, denoted  $v_{sa}$ ,  $v_{sb}$ ,  $v_{sc}$  and  $i_{c1}$ ,  $i_{c2}$ ,  $i_{c3}$ . The Concordia transformation makes it possible to reduce this balanced three-phase system to a two-phase system whose axes are in quadrature:

$$\begin{bmatrix} V_{sa} \\ V_{sb} \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & \frac{\sqrt{3}}{2} & -\frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} V_{sa} \\ V_{sb} \\ V_{sc} \end{bmatrix} \quad (1)$$

$$\begin{bmatrix} I_{sa} \\ I_{sb} \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & \frac{\sqrt{3}}{2} & -\frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} I_{ca} \\ I_{cb} \\ I_{cc} \end{bmatrix} \quad (2)$$

Instantaneous active power  $p$  and instantaneous reactive power  $q$  are defined by:

$$\begin{bmatrix} p \\ q \end{bmatrix} = \begin{bmatrix} v_{\alpha} & v_{\beta} \\ -v_{\beta} & v_{\alpha} \end{bmatrix} \begin{bmatrix} i_{\alpha} \\ i_{\beta} \end{bmatrix} \quad (3)$$

Instantaneous active and reactive powers can be written as the sum of a DC component and an AC component:

$$\begin{bmatrix} p \\ q \end{bmatrix} = \begin{bmatrix} \bar{p} + p \\ \bar{q} + q \end{bmatrix} \quad (4)$$

From equation (4), we can deduce the expressions for the components of the charging current along the  $\alpha\beta$  axes:

$$\begin{aligned} \begin{bmatrix} i_{\alpha} \\ i_{\beta} \end{bmatrix} &= \begin{bmatrix} V_{\alpha} & V_{\beta} \\ -V_{\beta} & V_{\alpha} \end{bmatrix}^{-1} \begin{bmatrix} p \\ -q \end{bmatrix} \\ \Rightarrow \begin{bmatrix} i_{\alpha} \\ i_{\beta} \end{bmatrix} &= \frac{1}{V_{\alpha}^2 + V_{\beta}^2} \begin{bmatrix} V_{\alpha} & -V_{\beta} \\ V_{\beta} & V_{\alpha} \end{bmatrix} \begin{bmatrix} p \\ -q \end{bmatrix} \end{aligned} \quad (5)$$

By replacing (4) in (5), these currents are expressed along the  $\alpha\beta$  axes by:

$$\begin{bmatrix} i_{\alpha} \\ i_{\beta} \end{bmatrix} = \frac{1}{V_{\alpha}^2 + V_{\beta}^2} \begin{bmatrix} V_{\alpha} & -V_{\beta} \\ V_{\beta} & V_{\alpha} \end{bmatrix} \begin{bmatrix} \bar{p} \\ -\bar{q} \end{bmatrix} + \frac{1}{V_{\alpha}^2 + V_{\beta}^2} \begin{bmatrix} V_{\alpha} & -V_{\beta} \\ V_{\beta} & V_{\alpha} \end{bmatrix} \begin{bmatrix} p \\ -q \end{bmatrix} \quad (6)$$

Finally, it is easy to obtain the reference currents along the abc axes by the inverse transformation of Concordia:

$$\begin{bmatrix} i_{ref1} \\ i_{ref2} \\ i_{ref3} \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & 0 \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} i_{ref\alpha} \\ i_{ref\beta} \end{bmatrix} \quad (7)$$

Figure 3 gives the implementation algorithm of the instantaneous power method to obtain the reference currents. The two-phase current method works in the space of  $\alpha\beta$  currents. It therefore requires fewer calculations while being more precise and more robust than other methods.

a change of reference point of the load currents and the network voltages is carried out using Concordia to switch from three-phase to two-phase ( $\alpha\beta$ ). Afterwards the reactive and active powers are calculated. At this stage, to obtain the AC components, two low-pass filters are used respectively for the active and reactive power. The calculation of the reference currents in the  $\alpha\beta$  benchmark is carried out thanks to the alternating components of the powers of the voltage and of the regulated voltage of the inverter. Finally to obtain the final result we apply the inverse transform of Concordia

:

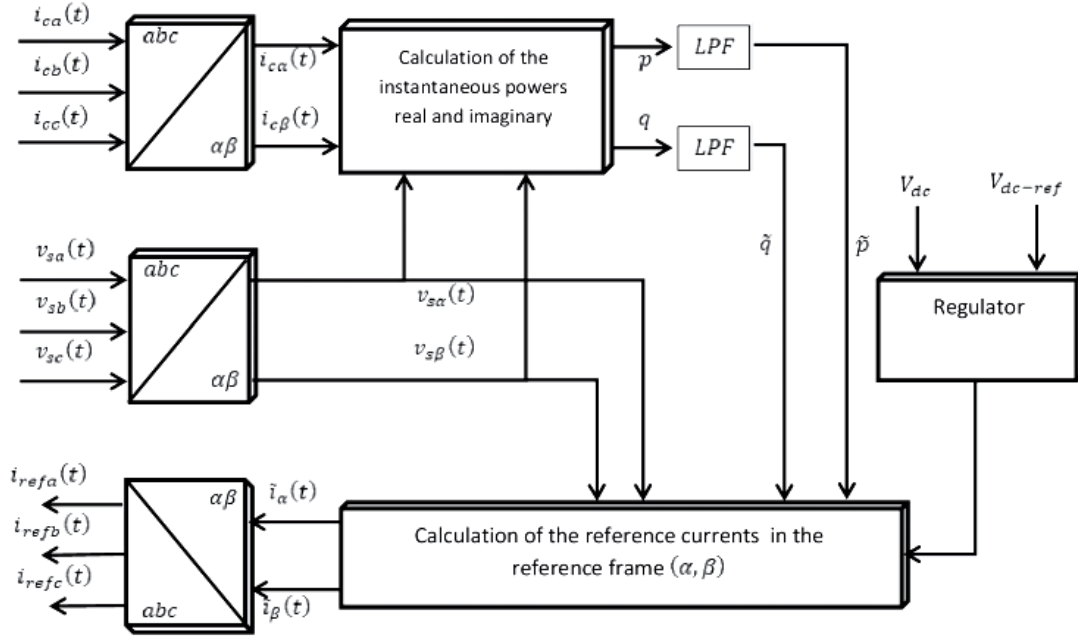


Figure 3: Generation of reference currents by the instantaneous power method

### C. Control by PWM of the active filter invert

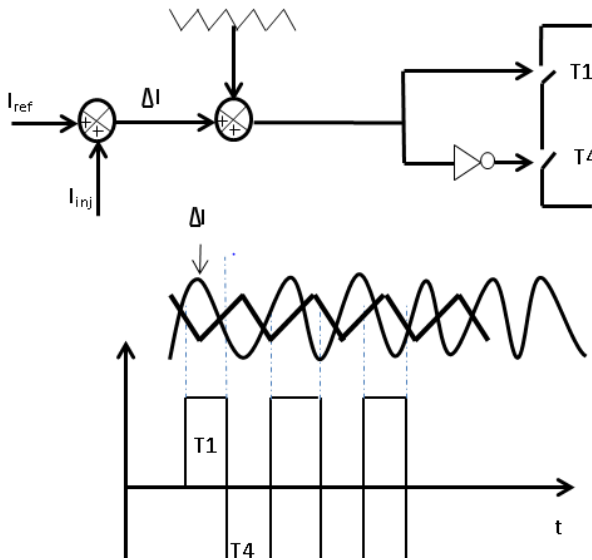


Figure 4: PWM control principle

In [20] the different PWM techniques are presented: the PWM with symmetric regular sampling, the PWM with asymmetric regular sampling and the PWM with natural sampling. The technical diagram of the PWM is given in Figure 4 each group of transistor-diode assembled in parallel forms a bi-controllable switch. The previous technical diagram first uses a regulator which determines the reference voltage of the inverter (modulator) from the difference between the measured current and its reference. The latter is then compared with a triangular signal called a high frequency carrier in this work it is a 200 Hz setting the switching frequency. The output of the comparator provides the command order of the switches. Figure 5 gives the Simulink model of the PWM control where the reference currents come from the instantaneous power unit PQ.

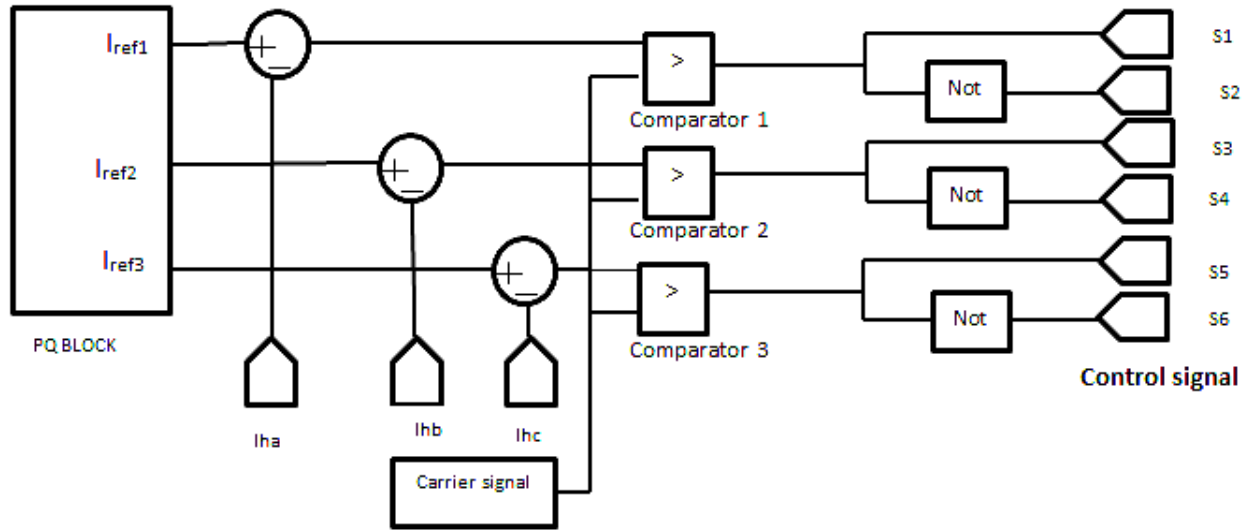


Figure 5: Command by PWM in MATLAB/SIMULINK

#### D. Control by DCM of the inverter of the active three-phase shunt filter

The duty cycle modulation technique (DCM) translates new perspectives in inverter control techniques. DCM consists in transforming a signal  $V_{ref}$  (reference intensity) into a modulated signal  $V_s(t)$ ,  $\pm V_{cc}$ , produces an all-or-nothing modulated signal, thus protecting the transmitted signal from noise. Non-inverting DCM is used in this case because it varies according to the modulation signal. Its operating principle is described in figure 6

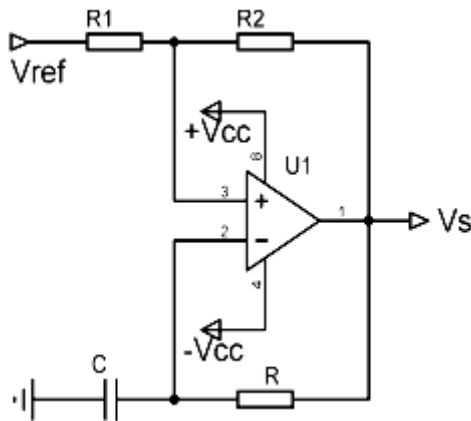


Figure 6: Non-inverter duty-cycle modulator [17]

The principle of duty cycle modulation (DCM) is based on encoding in the duty cycle  $R_m = T_{on}(t)/T_m(t)$  of a square wave signal of the reference analog signal  $V_{ref}(t)$ . A DCM circuit therefore behaves like a voltage controlled oscillator. It consists therefore in a modulator involving a high relaxation frequency of the oscillator and a low frequency of the control signal to be modulated. Thus, the resulting modulated

voltage  $V_s(t)$  is related to the associated switching control signal, the switching being ensured by an operational amplifier in its non-linear operation. The saturation voltages of the amplifiers are  $+V_{sat}$  and  $-V_{sat}$  while  $+V_{CC}$  and  $-V_{CC}$  are their supply voltages. The mathematical model DCM in our shunt filter is

$$V_s(t) = \begin{cases} V_{sat} & \text{if } u^+ > u^- \\ -V_{sat} & \text{if } u^+ < u^- \end{cases} \quad (8)$$

$$\Rightarrow u^+ = \begin{cases} \alpha V_{sat} + \alpha_1 V_{ref} & \text{if } V_s(t) = V_{sat} \\ -\alpha V_{sat} + \alpha_1 V_{ref} & \text{if } V_s(t) = -V_{sat} \end{cases}$$

With

$$\alpha = \frac{R_1}{R_1 + R_2} \quad (9)$$

$$\alpha_1 = \frac{R_2}{R_1 + R_2}$$

The supply voltage of the capacitor is governed by a differential equation:

$$RC \frac{du_c(t)}{dt} + u_c(t) = V_s(t) \quad (10)$$

A solution of this equation is:

$$u_c(t) = (u_i - u_f)e^{-t/RC} + u_f \quad (11)$$

The capacitor charge and discharge times are included respectively  $0 < t < T_1$  and  $T_1 < t < T_2$ . It is established that:

$$T_1 = -\tau \ln \left( \frac{\alpha_1 V_{ref} + (\alpha - 1)V_{sat}}{\alpha_1 V_{ref} - (1 - \alpha)V_{sat}} \right) \quad (12)$$

$$T_2 = -\tau \ln \left( \frac{\alpha_1 V_{ref} - (\alpha - 1)V_{sat}}{\alpha_1 V_{ref} + (1 + \alpha)V_{sat}} \right) \quad (13)$$

$$T = \tau \ln \frac{\alpha_1 V_{ref} - (\alpha - 1) V_{sat}}{\alpha_1 V_{ref} + (1 + \alpha) V_{sat}} + \tau \ln \frac{\alpha_1 V_{ref} + (\alpha - 1) V_{sat}}{\alpha_1 V_{ref} - (1 - \alpha) V_{sat}}$$

$$\Rightarrow T = RC \ln \left( \frac{(\alpha_1 V_{ref})^2 - ((\alpha - 1) V_{sat})^2}{(\alpha_1 V_{ref})^2 - ((1 - \alpha) V_{sat})^2} \right) \quad (14)$$

$$\tau = RC$$

The duty cycle of the non-inverting modulator is:

$$R_m = \frac{T_1(V_{ref})}{T_m(V_{ref})} \quad (15)$$

we deduct:

$$R_m(V_{ref}, \alpha, V_{sat}) = \frac{\ln \left( \frac{\alpha_1 V_{ref} - (\alpha - 1) V_{sat}}{\alpha_1 V_{ref} + (1 + \alpha) V_{sat}} \right)}{\ln \left( \frac{(\alpha_1 V_{ref})^2 - ((\alpha + 1) V_{sat})^2}{(\alpha_1 V_{ref})^2 - ((1 - \alpha) V_{sat})^2} \right)} \quad (16)$$

In order to improve the efficiency of the electronic parts of the non-inverting DCM modulator, we are optimizing our modulator. The aim is to find the optimal characteristic parameters  $\alpha$ ,  $\tau$  and  $E$  of the modulator providing an excellent level of operation. For this purpose, the effects of non-linearity and variation of the characteristic parameters were studied. The optimal quality of the modulator obtained is observed through its characteristic quantities:  $R_m(V_{ref}, \alpha, V_{sat})$  and  $f_m = \frac{1}{T(V_{ref}, \alpha, V_{sat}, \tau)}$

with  $f_m$  being the frequency of the modulator and  $R_m(V_{ref}, \alpha, V_{sat})$  the duty cycle.

Optimizing the MRC modulator therefore means maximizing  $P_m(\alpha, V_{sat})$  or minimizing  $-P_m(\alpha, V_{sat})$

Which is the slope. Our optimization criterion is therefore  $P_m(\alpha, V_{sat})$  or

$$P_m = \frac{\alpha}{V_{sat} (1 + \alpha) \log \left( \frac{1 + \alpha}{1 - \alpha} \right)} \quad (17)$$

$$\left\{ \begin{array}{l} f_{m0} = \frac{1}{2\tau \ln \left( \frac{1 + \alpha}{1 - \alpha} \right)} \\ f_{min} = \frac{1}{\tau \ln \left[ \frac{(\alpha_1 V_{max})^2 - ((1 + \alpha) V_{sat})^2}{(\alpha_1 V_{max})^2 - ((\alpha - 1) V_{sat})^2} \right]} \\ 0 < \alpha < 1 \end{array} \right. \quad (18)$$

With the basic frequency of the modulator  $f_{m0}$  previously selected, the minimum frequency  $f_m$  previously established  $\alpha = 0.003081723734398$

$\tau = RC$  with  $f_{mlim}$  is the limit modulator frequency. Our work on optimization is based on the formulation given in [16] and for the chosen  $f_{m0}$  equal to 200 KHz, the frequency  $f_{mlim}$  is obtained by calculating  $f_{min}$  for  $\alpha$  very small. We obtain the following optimum parameters of DCM:

$$\alpha = 0.003081723734398 \text{ or}$$

$$\alpha = R_1 / (R_1 + R_2) \text{ and } 1 - \alpha = R_2 / (R_1 + R_2)$$

After calculating the value  $\tau = 0.000486670905896s$ ,  $R_1 = 330\Omega$ ,  $R_2 = 10K\Omega$ ,  $C = 47nF$ ,  $R = 1K\Omega$

Figure.7 represents the Simulink diagram of the DCM modulator. The latter's input is  $I_{ref}$  and its output is  $cmd$ . Its parameters were determined in the previous paragraph.

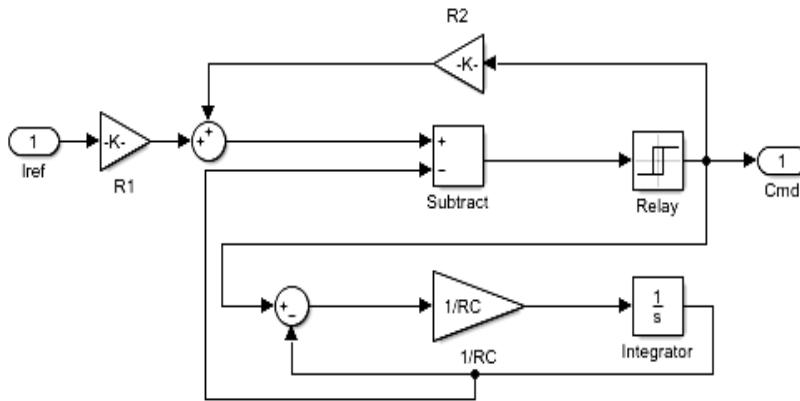


Figure 7: Command by DCM in MATLAB/SIMULIN

### E. Symmetrical Linear Duty-Cycle Modulation

Figure. 8 gives the operating principle of the SLDCM. The hysteresis comparator obtained the signal and the integrator modulates by integrating the difference between the modulated signal and the reference signal, a triangular signal is a return to the input of the comparator.

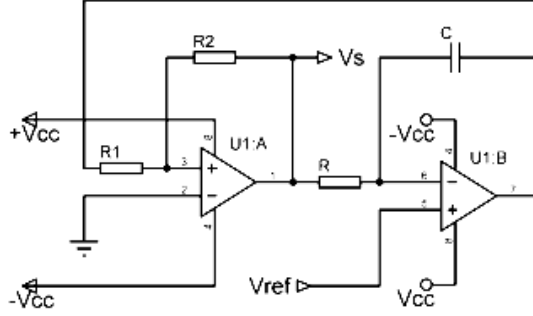


Figure 8: Symmetrical Linear Duty-Cycle Modulation [17]

The mesh law applied to the voltages on the first non-inverting modulator gives the equations below:

$$v_o R_2 + V_s R_1 = 0 \quad (19)$$

$$v_o = -\frac{R_1}{R_2} V_s \quad (20)$$

$v_o$  represents both the integrator output voltage and the input to the control signal switching block. The current in the capacitor C is defined by:

$$\begin{aligned} v_0^+ &= +\frac{R_1}{R_2} V_{sat} \\ v_0^- &= -\frac{R_1}{R_2} V_{sat} \end{aligned} \quad (21)$$

The current in the capacitor C is defined by:

$$i_c = \frac{V_s - V_{ref}}{R} = C \frac{dv_c}{dt} \quad (22)$$

Where,  $v_c$  is the voltage across the capacitor. The output voltage  $v_0$  of the integrator is given by:

$$\begin{aligned} v_0 &= V_{ref} - v_c \\ \Leftrightarrow v_c &= V_{ref} - v_0 \end{aligned} \quad (23)$$

So,

$$dt = \frac{RC}{V_s - V_{ref}} (dV_{ref} - dv_0) \quad (24)$$

If  $dV_{ref} = 0$  then  $V_{ref}$  is a constant so

$$dt = -\frac{RC}{V_s - V_{ref}} dv_0 \quad (25)$$

Now let's calculate  $t_{on}$  and  $t_{off}$

During  $t_{on}$ ,  $V_s = +V_{sat}$  and  $v_0$  goes from  $v_0^+$  to  $v_0^-$

$$t_{on} = -\frac{RC}{V_{sat} - V_{ref}} \int_{v_0^+}^{v_0^-} dv_0 \quad (26)$$

$$t_{on} = 2RC \frac{R_1}{R_2} \frac{V_{sat}}{V_{sat} - V_{ref}} \quad (27)$$

During  $t_{off}$ ,  $V_s = -V_{sat}$  and  $v_0$  goes from  $v_0^-$  to  $v_0^+$

$$t_{off} = 2RC \frac{R_1}{R_2} \frac{V_{sat}}{V_{sat} + V_{ref}} \quad (28)$$

$$\text{So, } T = t_{on} + t_{off} \quad (29)$$

$$T = 4RC \frac{R_1}{R_2} \frac{V_{sat}^2}{V_{sat}^2 - V_{ref}^2} \quad (30)$$

$\alpha$  Which represents the duty cycle is equal to:

$$\alpha = \frac{t_{on}}{T} = \frac{1}{2} \left( 1 + \frac{V_{ref}}{V_{sat}} \right) \quad (31)$$

The duty cycle of SLDCM is a linear equation (30) consisting only of the passive components. When  $V_{ref} = 0$  the respective values of its minimum periods and are duty cycles are equal to:

$$\begin{aligned} T_0 &= 4RC \frac{R_1}{R_2} \\ \alpha &= \frac{1}{2} \end{aligned} \quad (32)$$

## III. SIMULATION AND RESULTS

### A. Simulation parameter

Simulations in MATLAB/SIMULINK were carried out under the specifications found in Table 1 below.

The parameters of the simulations are grouped together in table 1. Regarding the DCM parameters, we use the data from [16] whose optimization parameters were determined in section II with a frequency of 200 hz. on the other hand the parameters of the SLDCM use the data of [17] which were provided experimentally in this article. The frequency value of SLDCM is 200HZ. Finally, the frequency of the PWM carrier is 200Hz compared to a frequency of 50Hz to produce the IGBT control slots.

The simulated electrical network is three-phase three-wire and the MATLAB/Simulink software is used. The pollutant load is a conventional three-phase rectifier connected in series in an electrical network

TABLE 1: SIMULATION PARAMETERS

|        |                                                                                                |
|--------|------------------------------------------------------------------------------------------------|
| Source | $V_s=220V, f=50Hz,$<br>$R_s=0.25 \times 10^{-3}\Omega$                                         |
| Load   | $L_c=0.023\text{ mH},$<br>$R_c=0.82\text{m}\Omega, =0.78\text{m}\Omega,$<br>$L_c=2.6\text{mH}$ |
| Filter | $L_f=3\text{mH}, C=8\text{mF}$                                                                 |
| DCM    | $R1=330\Omega, R2=10\text{K}\Omega,$<br>$C=47\text{nF}, R=1\text{K}\Omega$                     |
| SLDCM  | $R1=10\text{K}\Omega, R2=20\text{K}\Omega,$<br>$C=10\text{nF}, R=5.000\text{K}\Omega$          |

The general structure of the studied system is given in Figure. 9, the system is constituted:

- A three-phase power source,
- A non-linear charge,
- An active three-phase shunt filter connected in parallel to the mains,
- A filter control unit.

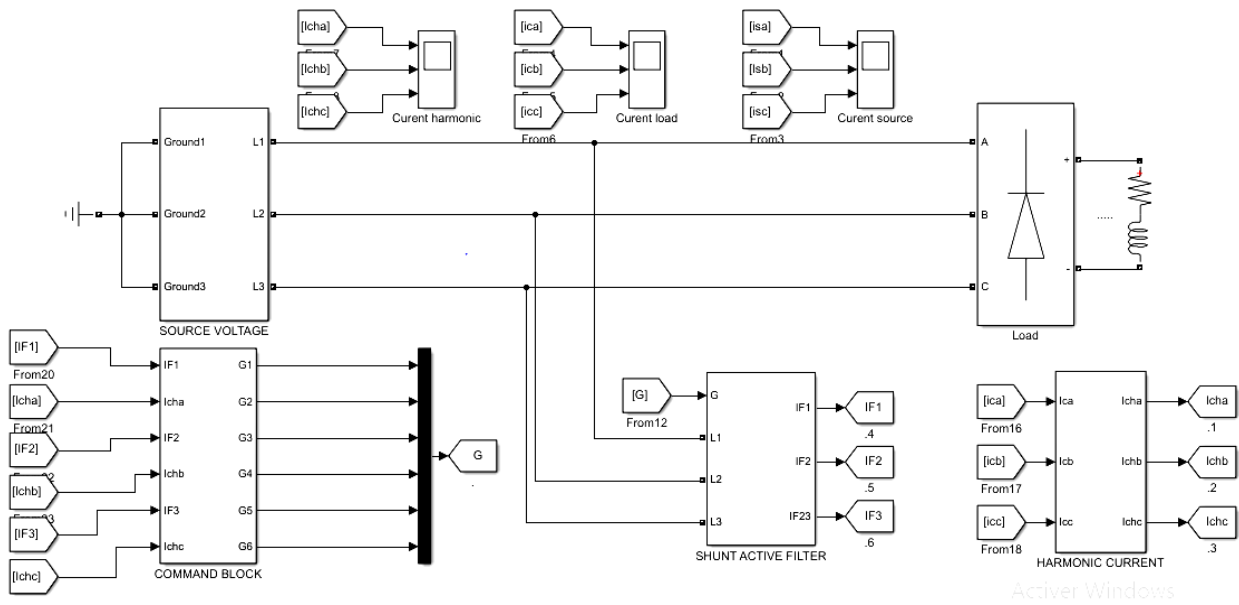
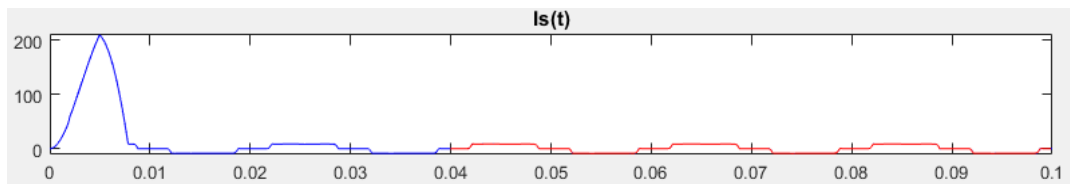


Figure 9: The general structure of the system studied

Figure 10: Waveform of the load and source  $I_s(t)$  before filter

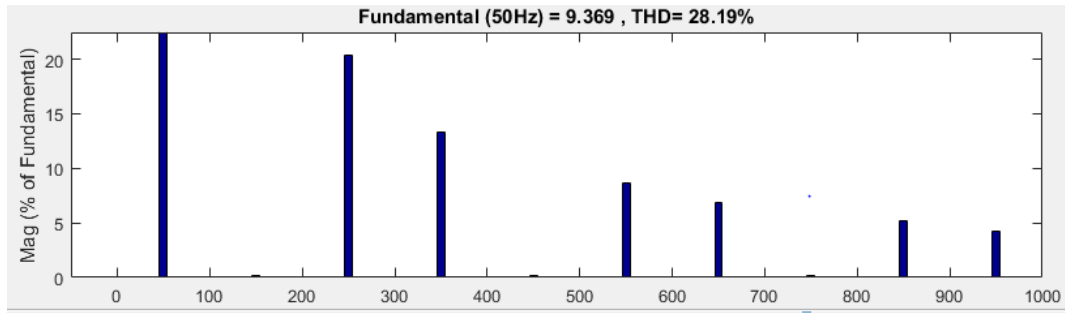


Figure 11: Order of source current harmonics and TDH before shunt active filter

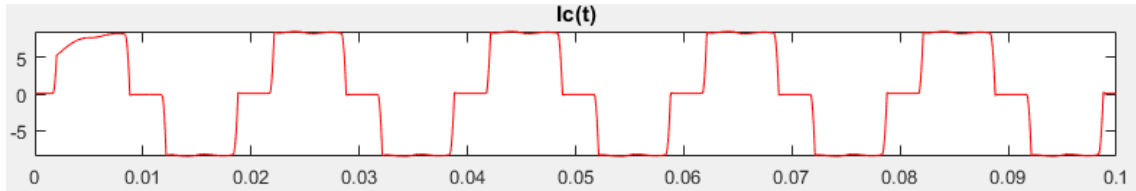


Figure 12: Waveform of the load

Figure. 10 shows the course of the current  $I_s(t)$  in the network before filtering for phase (a), the spectral analysis of this current is presented in Figure. 11 source harmonics spectrum contains the harmonics of rank 5,7,13,17 and 19. And we observe the presence of several ranks of harmonics disturbing the current

waveform, i.e. a THD of 28.197%. Figure. 12 is a waveform of the load current main actors of said deformations because it does not consume the sinusoidal energy produced by the source it then injects into the circuit of harmonics.

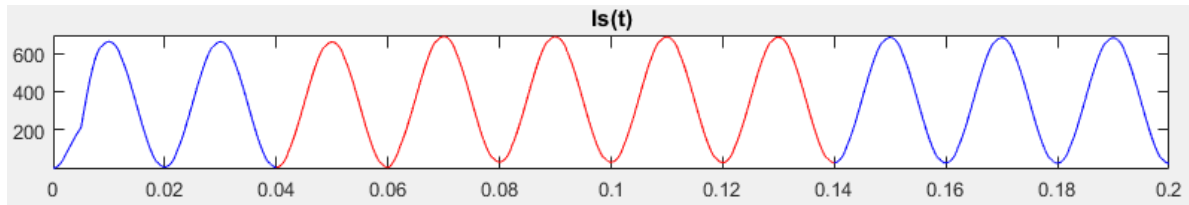
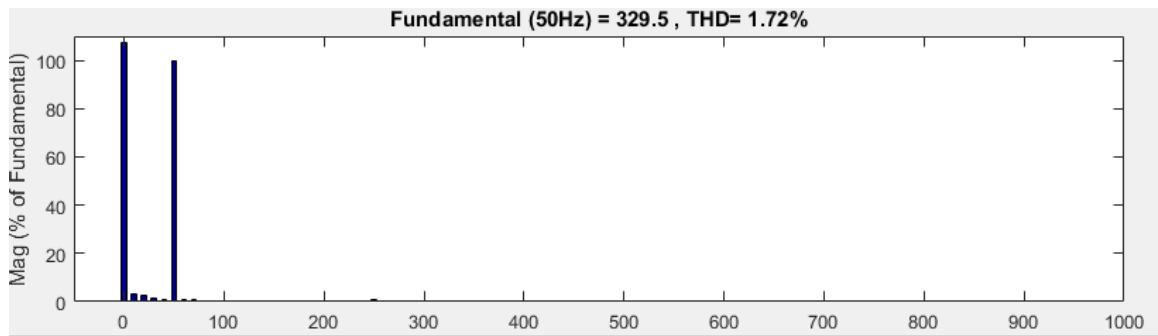
Figure 13: Waveform of the current source  $I_s(t)$  after filter: control by PWM

Figure 14: Order of source current harmonics and TDH after shunt active filter: control by PWM

Figure. 13 and 14 are the characteristics obtained from the source current after filtering using the PWM control, thus obtaining respectively the waveform which has become sinusoidal again, proof that there has been a reduction in harmonics and the harmonic rate which has passed from 28.19% THD to 1.72%, the result of which complies with the IEEE-519 standard which must meet the condition that the THD must be less than 5%.

After filtering the current  $I_s(t)$  by the active shunt filter controlled by PWM control, we obtain the signal in Figure. 13. We observe a significant improvement in the waveform which has become sinusoidal and whose spectrum given in Figure 14 allowing us to affirm that there is a clear decrease in harmonics, i.e. a THD of 1.72%.

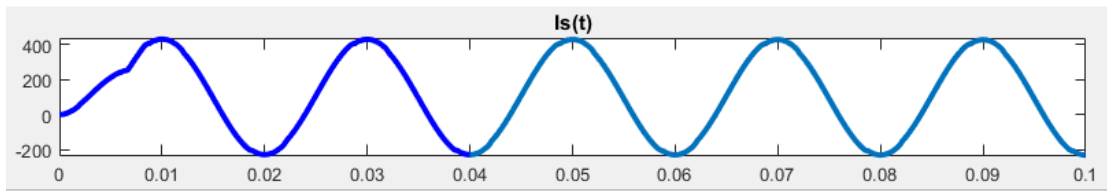
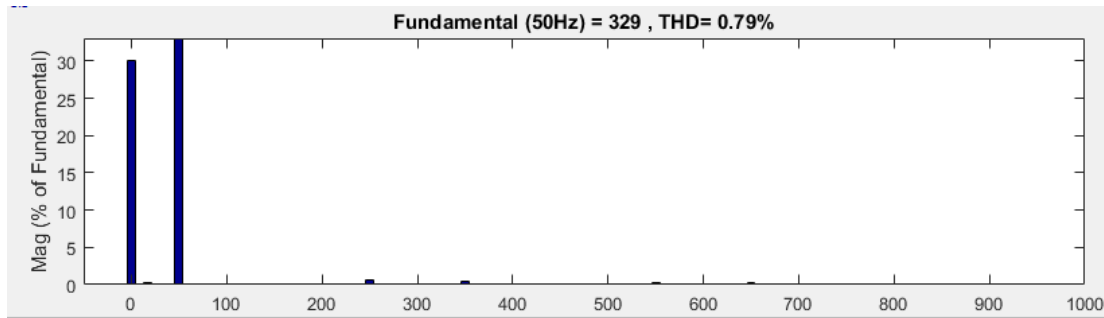
Figure 15: Waveform of the current source  $I_s(t)$  after filter: control by DCM

Figure 16: Order of source current harmonics and TDH after shunt active filter: control by DCM

By applying the control by Modulation with DCM to our active shunt filter we obtain the signal  $I_s(t)$  in Figure 15 which shows a significant improvement in

the curve and whose current spectrum  $I_s(t)$  in Figure 16 shows a greater reduction in harmonics, i.e.  $THD = 0.79\%$ .

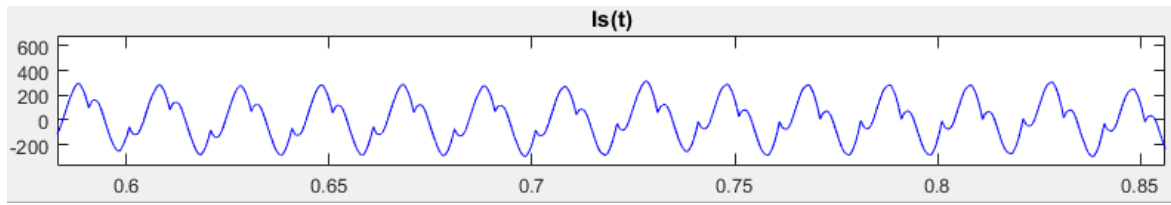
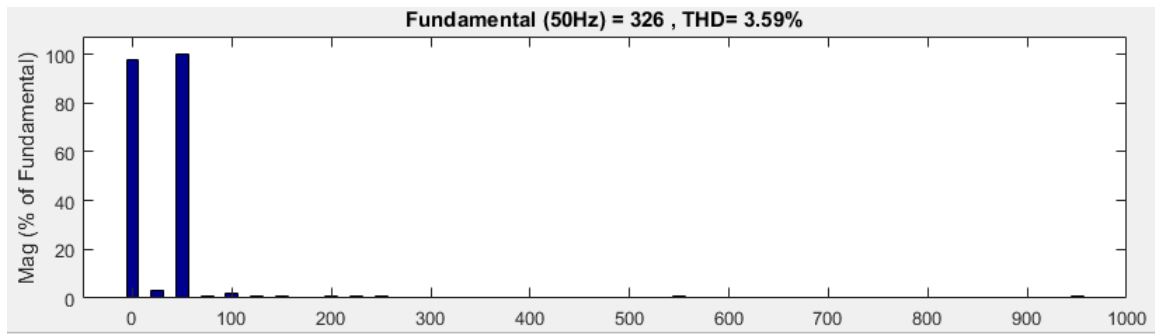
Figure 17: Waveform of the current source  $I_s(t)$  after filter: control by SLDCM

Figure 18: Order of source current harmonics and TDH after shunt active filter: control by SLDCM

By applying the control by Modulation with SLDCM to our active shunt filter we obtain the signal  $I_s(t)$  in Figure 17 which shows a slight degradation at

the level of the curve and whose current spectrum  $I_s(t)$  in Figure 18 shows a reduction in harmonics of less than 5%, that is to say  $THD = 3.59\%$ .

TABLE 2: INTERPRETATION OF PERFORMANCE FOR THE TWO ORDERS

|                                            | PWM Control | DCM Control | SLDCM Control |
|--------------------------------------------|-------------|-------------|---------------|
| THD before filtering                       | 28,19%      | 28,19%      | 28,19%        |
| THD after filtering                        | 1.72%       | 0.79%       | 3.59%.        |
| Main voltage                               | 220V        | 220V        | 220V          |
| Controllability of the switching frequency | good        | good        | Bad           |
| Waveform of output current $I_s$           | good        | Good        | Fairly good   |

Table 2 gives an interpretation of the results obtained for Hysteresis and Cyclic Ratio Modulation (DCM) control. THD of the current at phase (a)  $I_s(t)$  after filtering calculated on the first 20 harmonic ranks is 1.72% for PWM control, 0.79% for DCM control, and 3.59% for SLDCM which corresponds to the IEEE 519 standard that limits the THD < 5%, but it can be seen that control by DCM has better performance in terms of harmonic elimination, it is easy to use, ensures operation at a fixed frequency.

### CONCLUSION

In this article, we have presented the method of instantaneous powers for the creation of disturbance currents; a mathematical model has been developed. We used PWM control DCM and SLDCM commands for switching IGBTs. Their principle is based on the modulation of a reference voltage. This voltage, called the modulating signal at the input of the modulator, will be transposed into a modulated signal in the form of square waves representing the control signals of the IGBTs. These two systems were implemented and observed under the same conditions in an active shunt filter. Regarding the THD rate in the electrical circuit, the DCM gives the best performance because it is 0.79% against 1.72% for the PWM and 3.59% for SLDCM. but it can be seen that the DCM control has better performance in terms of harmonic elimination and is positioned in the literature as a promising method due to its flexibility and ease of implementation in industrial applications. It will also be interesting to carry out an in-depth study between the intelligent controls techniques neural networks with DCM applied to control the inverter in an active shunt filter.

TABLE 3: COMPARISON OF METHODS IN THE LITERATURE

|                                                     | PWM<br>Intersective<br>Control<br>[21] | Hysteresis<br>Control<br>[16] | DCM<br>Control |
|-----------------------------------------------------|----------------------------------------|-------------------------------|----------------|
| Waveform of<br>output current                       | good                                   | Fairly<br>good                | good           |
| TDH before<br>filtering                             | 20,17%                                 | 26,57%                        | 28,19          |
| TDH after<br>filtering                              | 2.33%                                  | 3,12%                         | 0.79%          |
| Signal quality                                      | No noise                               | Brute                         | No noise       |
| Controllability<br>of the<br>switching<br>frequency | Yes                                    | No                            | Yes            |

The performance of the proposed active shunt filter control strategy was compared with the control strategy adopted with some other control methods proposed in the literature. Table 3 shows the comparison of various control techniques proposed in

the literature for harmonic reduction. It is clearly established that all these methods give a THD < 5% thus complying with the IEEE-519 standard, but the control strategy using DCM with the shunt active filter topology proposed in this work is more flexible due to its simplicity of implementation and allows good controllability of the switching frequency of the inverter switches that make up the active filter.

### NOMENCLATURE

|                          |                                                      |
|--------------------------|------------------------------------------------------|
| PWM                      | Pulse Wave Modulation                                |
| DCM                      | Duty Cycle Modulation                                |
| GLDCM                    | General linear Duty<br>Cycle Modulation              |
| LNIDCM                   | Linearized Non-<br>Inverter Duty Cycle<br>Modulation |
| NIDCM                    | Non-Inverter Duty<br>Cycle Modulation                |
| THD                      | Total Harmonic<br>Distorsion                         |
| $V_{ref}$                | Reference or control<br>voltage                      |
| $V_{sat}$                | Saturation voltage                                   |
| $V_{sa}, V_{sb}, V_{sc}$ | Output voltage                                       |
| $V_o$                    | Integrator output<br>voltage                         |
| $V_c$                    | Capacitor voltage                                    |

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